

**A Spektroszkópia 2. kollokviumon használható  
képletek gyűjteménye  
(2007)**

$$E(r,t) = \frac{1}{4\pi\epsilon_0} \frac{\ddot{p}\left(t - \frac{r}{c}\right) \sin\theta}{rc^2} \quad B(r,t) = \frac{1}{4\pi\epsilon_0} \frac{\ddot{p}\left(t - \frac{r}{c}\right) \sin\theta}{rc^3}$$

$$-\frac{dW}{dt} = \frac{\omega_0^4 e^2 z_0^2}{2} \frac{1}{6\pi\epsilon_0 c^3}$$

$$E(\omega) = \text{FT}\{E(t)\} \sim \left[ \frac{1}{i(\omega + \omega_0) - \left(\frac{\gamma_0}{2}\right)} + \frac{1}{i(\omega - \omega_0) - \left(\frac{\gamma_0}{2}\right)} \right]$$

$$I(\omega) \sim |E(\omega)|^2 \sim \frac{1}{(\omega - \omega_0)^2 + \left(\frac{\gamma_0}{2}\right)^2}$$

$$z_0 = -\frac{e}{m} \frac{E_0}{\omega_0^2 - \omega^2 + i\gamma\omega}$$

$$P = N \frac{e^2}{m} \frac{E}{\omega_0^2 - \omega^2 + i\gamma\omega}$$

$$n' = 1 + \frac{1}{2} \frac{Ne^2}{\epsilon_0 m} \frac{\omega_0^2 - \omega^2}{(\omega_0^2 - \omega^2)^2 + \gamma^2 \omega^2}$$

$$\kappa = \frac{Ne^2}{2\epsilon_0 m} \frac{\gamma\omega}{(\omega_0^2 - \omega^2) + \gamma^2 \omega^2}$$

$$\alpha = \frac{Ne^2}{c\epsilon_0 m} \frac{\gamma\omega^2}{(\omega_0^2 - \omega^2)^2 - \gamma^2 \omega^2}$$

$$\sigma(\omega) = \frac{e^2}{4m\epsilon_0 c} \frac{\gamma}{(\omega_0 - \omega)^2 + \left(\frac{\gamma}{2}\right)^2}$$

$$\int_0^\infty \sigma(\omega) d\omega = \frac{1}{2} \frac{e^2 \pi}{m\epsilon_0 c}$$

$$I_a = \int_0^\infty dI_a = \int_0^\infty I(\omega) N \sigma x d\omega = NxI(\omega_0) \int_0^\infty \sigma d\omega = NxI(\omega_0) \frac{1}{2} \frac{e^2 \pi}{m\epsilon_0 c}$$

$$n^2 = 1 + \sum_i \frac{a_i}{\lambda^{-2} - b_i}$$

$$\frac{dW}{dt} = \frac{\pi e^2}{2\epsilon_0 m} \sum_j f_{ij} \bar{N}_i \rho(\omega_{ji})$$

$$\bar{N}_i = \frac{g_i \exp\left(-\frac{E_i}{kT}\right)}{g_i \exp\left(-\frac{E_i}{kT}\right) + g_j \exp\left(-\frac{E_j}{kT}\right)} \bar{N} \quad \bar{N}_j = \frac{g_j \exp\left(-\frac{E_j}{kT}\right)}{g_j \exp\left(-\frac{E_j}{kT}\right) + g_i \exp\left(-\frac{E_i}{kT}\right)} \bar{N}$$

$$\rho(\omega) = \frac{\hbar \omega^3}{\pi^2 c^3 \exp\left(\frac{\hbar \omega_{ji}}{kT}\right) - 1}$$

$$W_{ij} = \frac{1}{\hbar} \langle \phi_i | H' | \phi_j \rangle$$

$$V_{12} = E_{0x} \frac{e}{\hbar} \langle \phi_1 | D_x | \phi_2 \rangle$$

$$i\dot{c}_1 = c_2 V_{12} \exp(-i\omega_{21}t) \cos \omega t$$

$$i\dot{c}_2 = c_1 V_{12}^* \exp(i\omega_{21}t) \cos \omega t$$

$$|c_2(t)|^2 = |V_{12}|^2 \frac{\sin^2 \frac{\omega_{21} - \omega}{2} t}{(\omega_{21} - \omega)^2}$$

$$\frac{d\langle |c_2(t)|^2 \rangle}{dt} = \frac{\pi e^2}{\epsilon_0 \hbar^2} \left| \langle \phi_1 | D_x | \phi_2 \rangle \right|^2 \rho(\omega_{21})$$

$$B_{12} = \frac{\pi e^2}{3\epsilon_0 \hbar^2} \left| \langle \phi_1 | \bar{D} | \phi_2 \rangle \right|^2$$

$$\frac{dN_2}{dt} = -A_{21} N_2 \int_0^\infty g(v) dv + B_{12} N_1 \int_0^\infty g(v) p(v) dv - B_{21} N_1 \int_0^\infty g(v) p(v) dv$$

$$\frac{dI_v}{\frac{c}{n} dt} = -B_{12} N_1 \frac{I_v}{\frac{c}{n}} g(v) \hbar v$$

$$\sigma_a = \frac{B_{12} g(v) \hbar v}{\frac{c}{n}}$$

$$\frac{dI_v}{dx} = -\sigma_a N_1 I_v + \sigma_e N_2 I_v + \frac{\hbar v}{\tau} N_2$$

$$g(h\nu) = \int_{-\infty}^{\infty} P_1(E)P_2(E + h\nu)dE$$

$$g(h\nu) = \frac{1}{2\pi} \frac{\Delta E_1 + \Delta E_2}{[h\nu - (E_2 - E_1)]^2 + \left(\frac{\Delta E_1 + \Delta E_2}{2}\right)^2}$$

$$\frac{dN}{N} = \sqrt{\frac{m}{2\pi kT}} \exp\left(-\frac{mv_z^2}{2kT}\right) dv_z$$

$$g(v) = \sqrt{\frac{m}{2\pi kT}} \frac{c}{v_{21}} \exp\left[\left(-\frac{m}{2kT} \frac{c^2}{v_{21}^2}\right)(v - v_{21})^2\right]$$

$$r_n = \frac{e^2}{8\pi\epsilon_0 hcR} \cdot \frac{n^2}{Z}$$

$$\frac{d^2(rR)}{dr^2} + \frac{2\mu rR}{\hbar^2} (E - E_{TK} - V(r)) = \Lambda^2 \frac{R}{r}$$

$$-\left(\frac{\partial^2 Y}{\partial \theta^2} + \text{ctg}\theta \frac{\partial Y}{\partial \theta} + \frac{1}{\sin^2 \theta} \frac{\partial^2 Y}{\partial \varphi^2}\right) = \Lambda^2 Y$$

$$Y_{l,m_l}(\theta, \varphi) = \sin^{|m_l|}(\theta) P_{l,m_l}(\cos \theta) e^{im_l \varphi}$$

$$E_n = -\frac{Z^2 \mu e^4}{32\pi^2 \epsilon_0^2 \hbar^2} \cdot \frac{1}{n^2} + E_{TK}$$

$$R_{n,l} = \rho^l L_{n,l}(\rho) e^{-\frac{\rho}{2}}$$

$$|\Psi|^2 4\pi r^2 dr = P(r) dr$$

$$d = s \frac{\partial Z}{m_a v_0^2} \mu_z$$

$$\boldsymbol{\mu} = -g \frac{e}{2m} \mathbf{L}$$

$$T = \frac{RZ^2}{n^2} + \frac{\alpha^2 RZ^4}{n^3} \left( \frac{1}{j + \frac{1}{2}} - \frac{3}{4n} \right) = T_0 + \Delta T$$

